

# **Constraint-Based Techniques for Managing Movement in Crowded Airspaces**

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# Acknowledgments

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# Outline of Talk

- Management of Crowded Airspaces
- Dynamic Airspace Deconfliction Project
  - Building Conflict-Free Movement Schedules
  - Integrating with distributed, real-time airspace deconfliction processes
- Future directions



# Airspace Deconfliction: Civilian Aviation

- Increasing volume of aircraft and congestion around airports
- Complexity of determining corridors and sequencing for takeoff, landing and holding

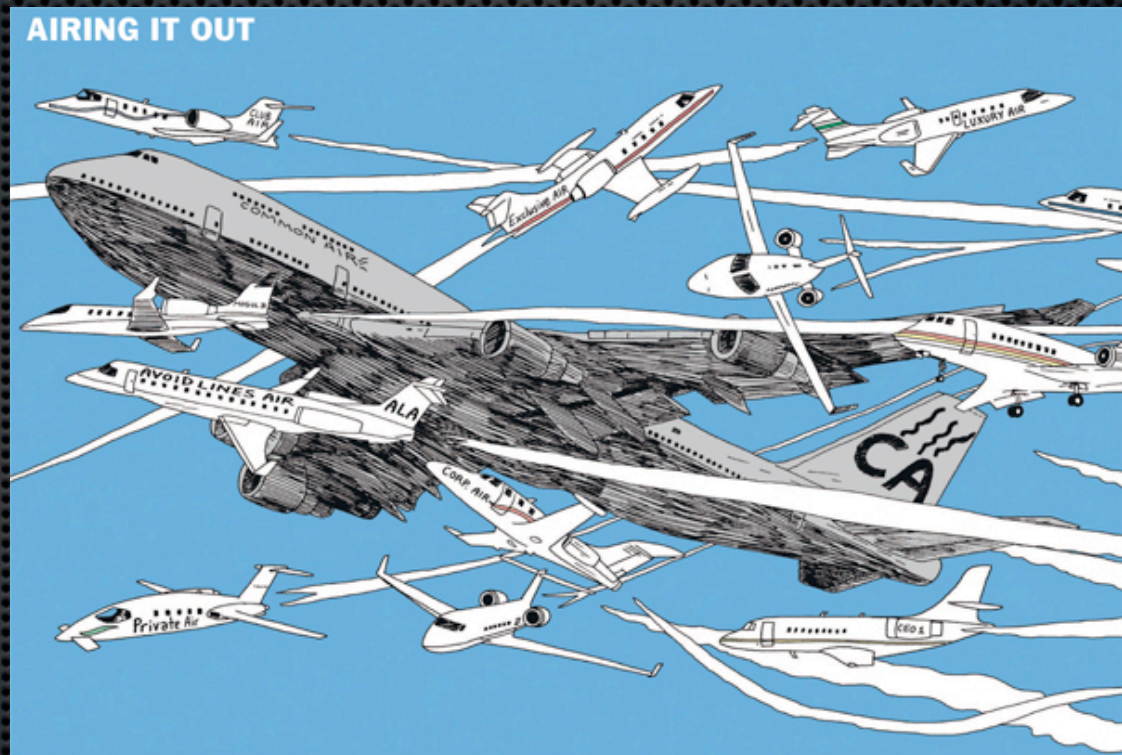
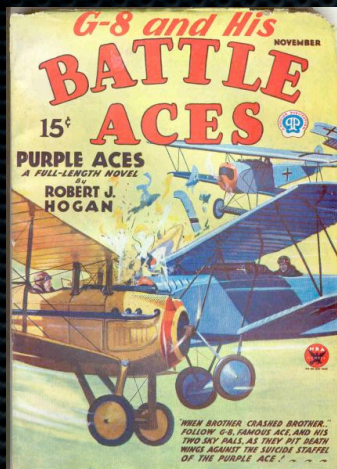


Illustration by Peter Arkle for the New York Times – 26 August 2007



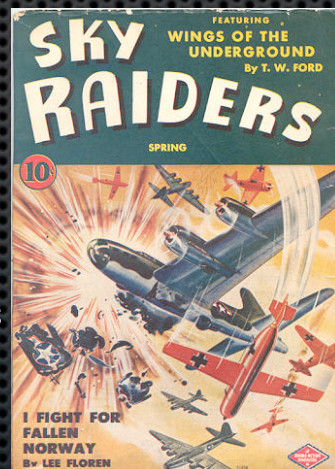
# Airspace Deconfliction: Military Aviation



1933



1935



1944

- Concurrent missions
- Localized and heavily populated environment
- Dynamically generated mission routes
- Increasingly autonomous aircraft
- Pop-up threats, friendly forces
- Strict partitioning of airspace is inefficient



# Emerging Concepts: Dynamic Airspace Configuration

- Automated separation assurance (via ground-based or distributed airborne systems)
- User-preferred trajectories
- Dynamic traffic management (adaptive speed control, route modification)
- Adaptable airspace to meet user demand, react to changing weather, maintain safety, etc.
- “DAC allocates airspace as a resource to meet user demand ...”<sup>1</sup>

1. P. Kopardekar, K. Bilimoria and B. Sridhar, “Initial Concepts for Dynamic Airspace Configuration”, *Proc. 7<sup>th</sup> AIAA Aviation Technology, Integration and Operations Conference*, Belfast, Sept. 2007



# Dynamic Airspace Deconfliction

*Joint Boeing–CMU research collaboration*

**Goal:** Technology components to support planning and execution of conflict-free air operations

## **Technical Approach:**

- Leverage previous work in constraint-based scheduling and task allocation
- Investigate and incorporate techniques for representing and reasoning about spatial constraints
- Couple mechanisms for centralized global mission planning with real-time distributed deconfliction processes



# Starting Point: Dynamic Task Allocation and Scheduling

**Core Technology:** *Incremental, Constraint-based Search*

**Applications:**

- **AMC Allocator** - day-to-day mgnt. of airlift & tanker missions

1. Generate Mission Schedules

2. Review Aircraft Commitment Levels

3. Compare Alternative (Re)Allocation Options

4. Identify Mission Merging Opportunities

5. Generate and Link Tanker Missions

- **ACS (Air Campaign Scheduler)** streaming ATO generation

1. Generate Mission Schedules

2. View Air Attacks from Sigonella

3. View Available Resource Capacity

4. Adjust Resource Availability Constraints

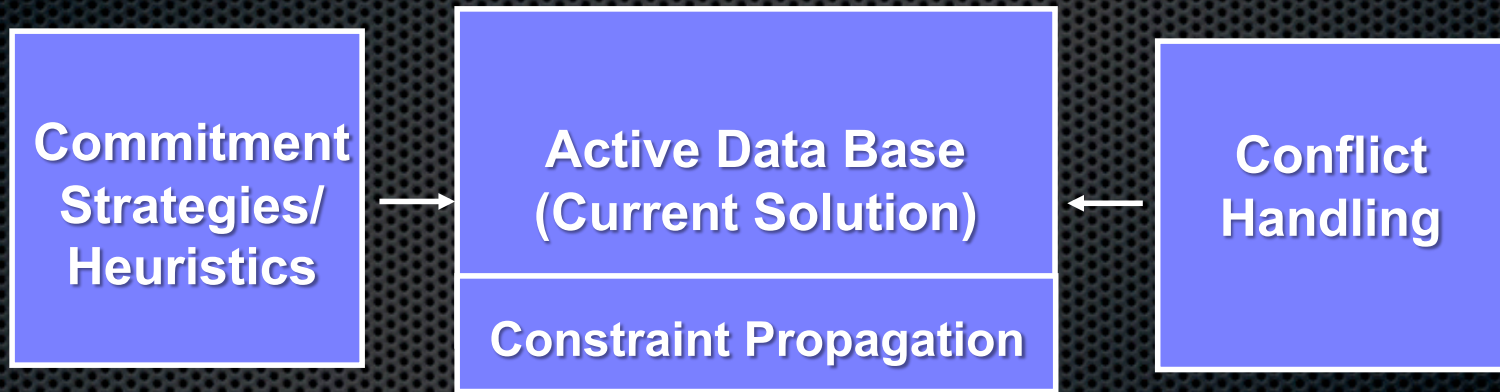
- **DARPA Coordinators** - distributed management of high-quality joint plans





# Constraint-Based Search Models

## Components:



## Properties:

- Modeling Generality/Expressiveness
- Incrementality
- Compositional



# Building Conflict-Free Movement Schedules

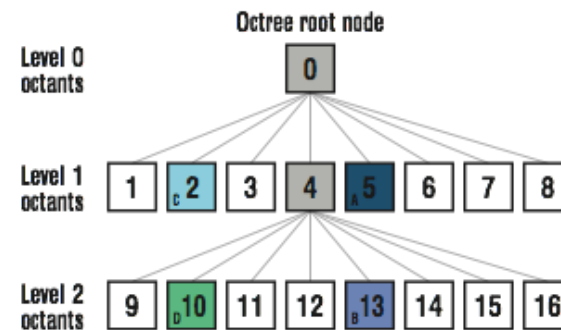
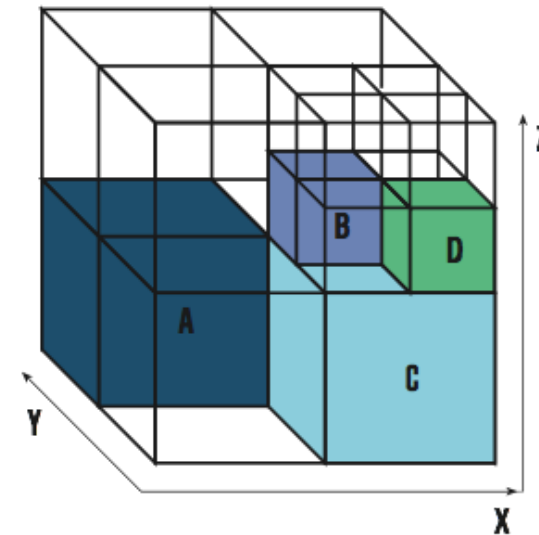
## Approach:

- View space as a *capacitated* resource and treat airspace deconfliction as an extended resource allocation problem
- Exploit *Octree* representation of air space volumes over time
- Generalize the notion of contention-based search heuristics
  - Construct and use a profile of spatial contention to make vehicle-routing and sequencing decisions



# The Octree

- Hierarchical, three-dimensional data structure (an extension of the 2D **quadtree**)
- Recursively subdivides a spatial volume into smaller subvolumes (called **octants**)
- Localizes common objects indexed by  $[x,y,z]$  coordinates





# The Linear Octree

- & Represents the octree as a balanced binary tree
- & Locational codes computed from the  $[x,y,z]$  coordinates of each octant's origin serve as keys in the binary tree
- & The result is a leaner and more efficient data structure



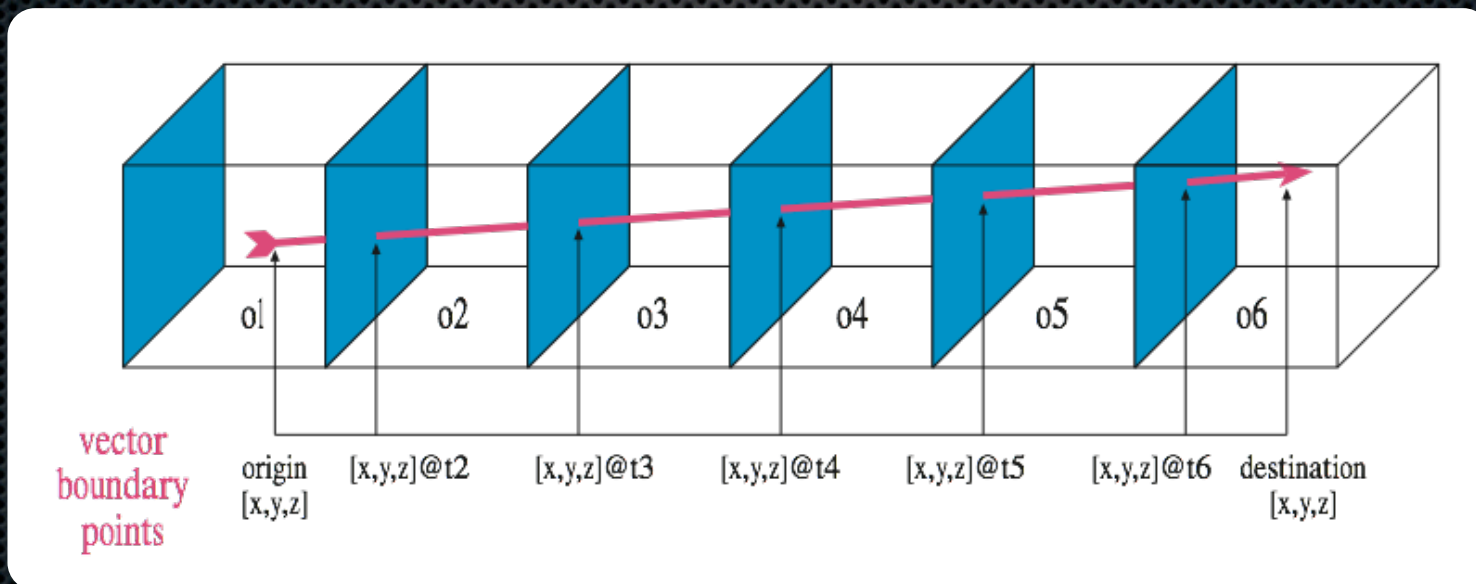
# Storage and Manipulation of Vehicle Routes

- Allocating vehicle routes to octants  
(a route is a sequence of 4D vectors)
- Determining conflicts using spherical MAZes (Maneuver Avoidance Zones) and the Closest Point of Approach



# Allocating Vehicle Routes to Octants

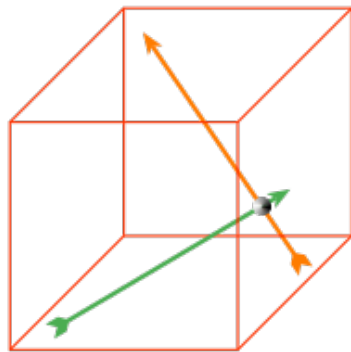
- Vectors are apportioned across all intersecting octants
- A conflict is signaled by the **spatial and temporal** overlap of two or more vector segments within an octant





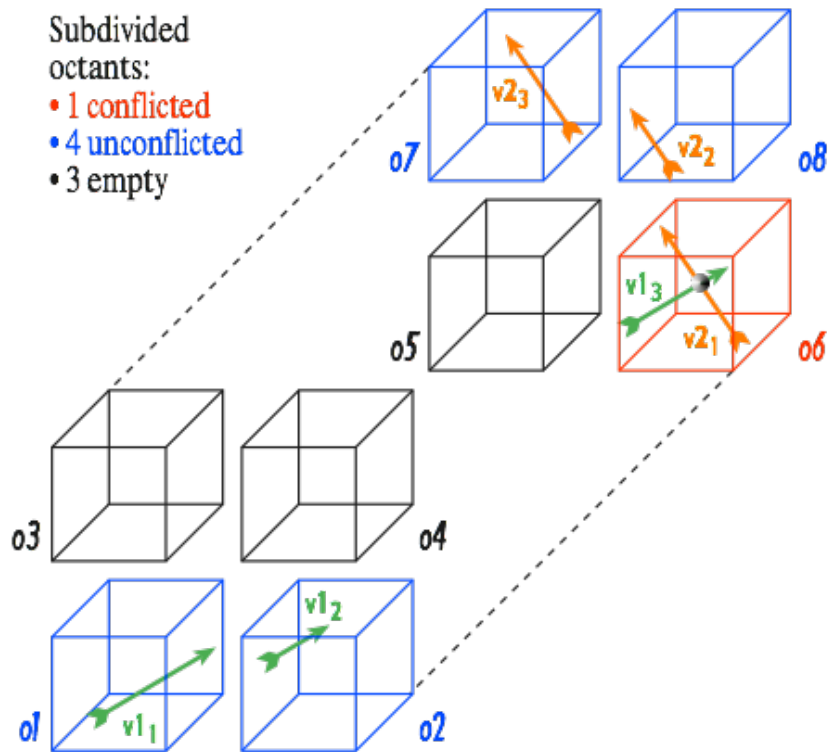
# Octant Subdivision in Response to a Conflict

Conflicted  
octant:



Intersecting vectors:  
 $v_1$  &  $v_2$  at  $\bullet$

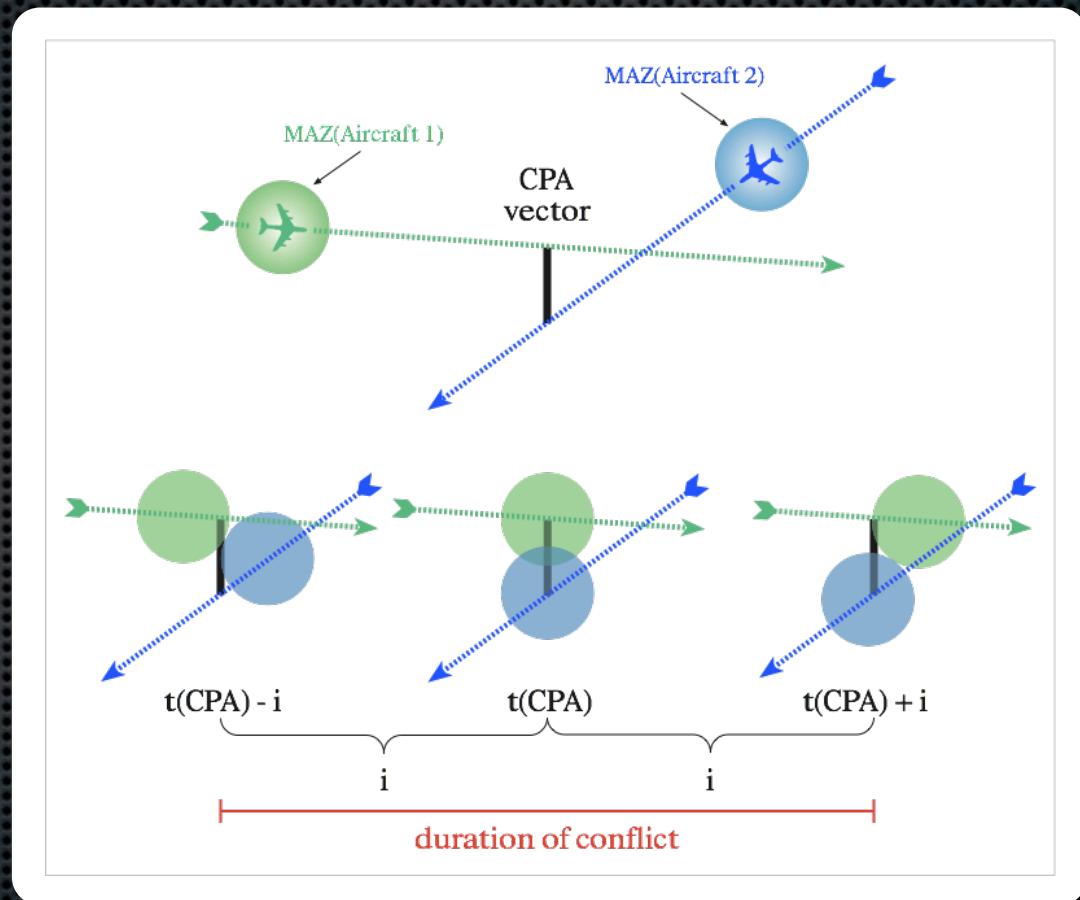
Subdivided  
octants:  
• 1 conflicted  
• 4 unconflicted  
• 3 empty





# Determining Conflicts

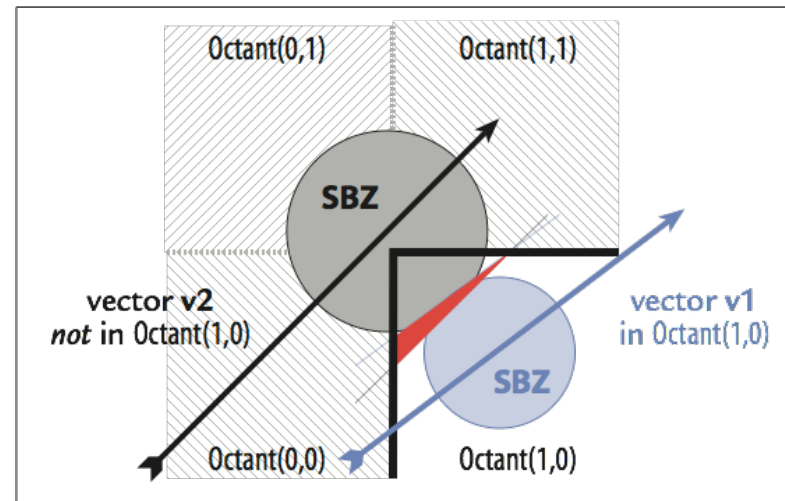
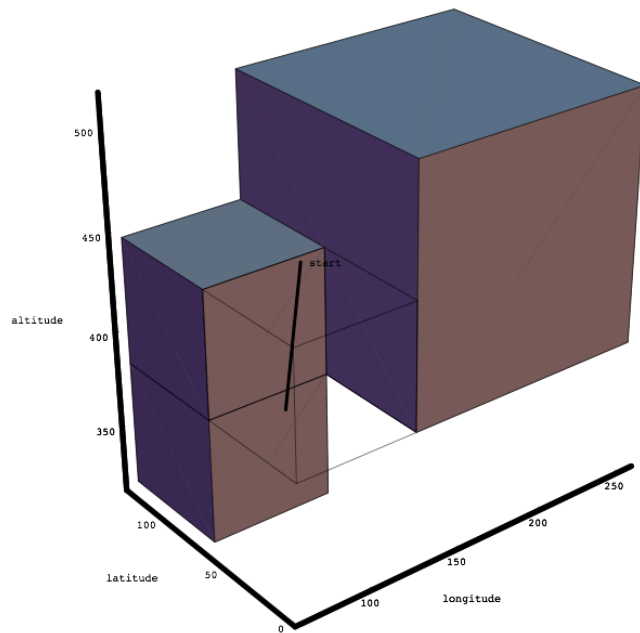
- A conflict between two vehicles is centered around the time of its closest point of approach (CPA)
- The duration of a conflict is measured from the beginning to the end of the spatial overlap





# Searching for Conflicts Among Neighboring Octants

- Neighboring octants must be searched for conflicting vectors whenever a vector is too close to an octant boundary



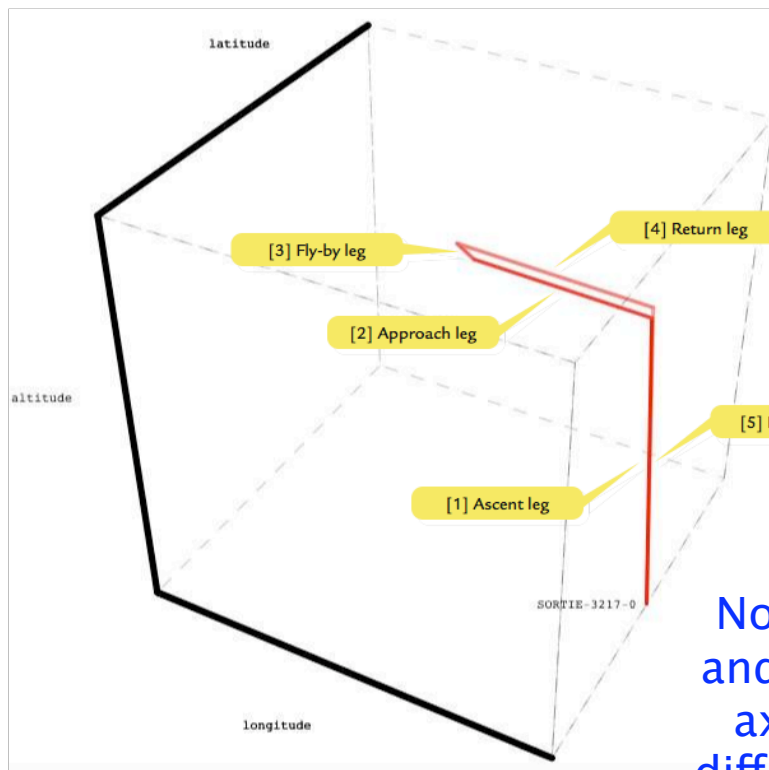


# Generating Conflict-Free Schedules

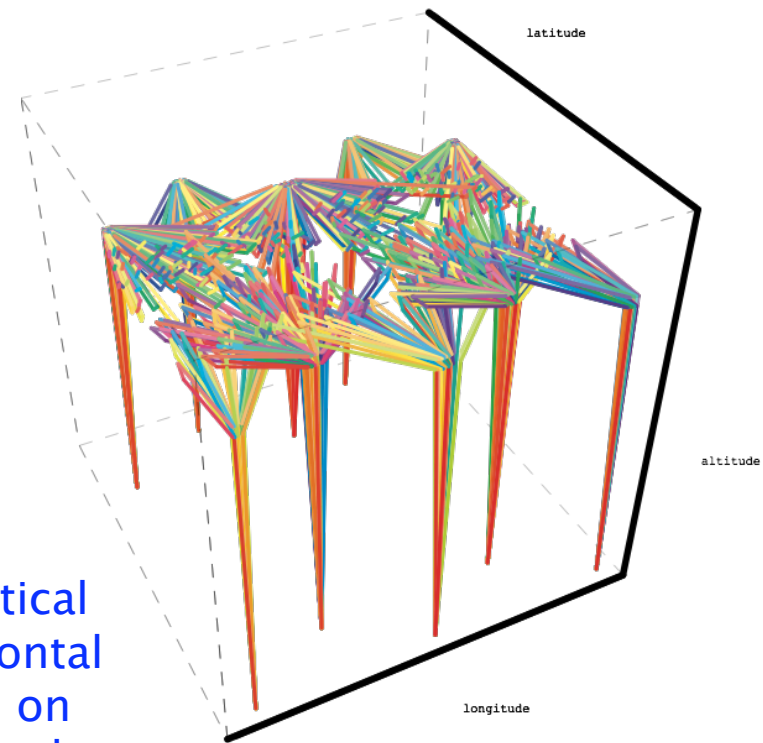
- **Approach:**
  - start with a base scheduling algorithm for computing a resource-feasible schedule for a set of itineraries
  - incorporate a route-planning component
  - extend algorithm to allocate space in the octree
- **Two phase schedule generation procedure:**
  - **priming** phase – build a resource-feasible schedule that ignores spatial capacity constraints
  - **scheduling** phase – use spatial contention profile to build extended solution that enforces spatial constraints



# Air Vehicle Mission Routes

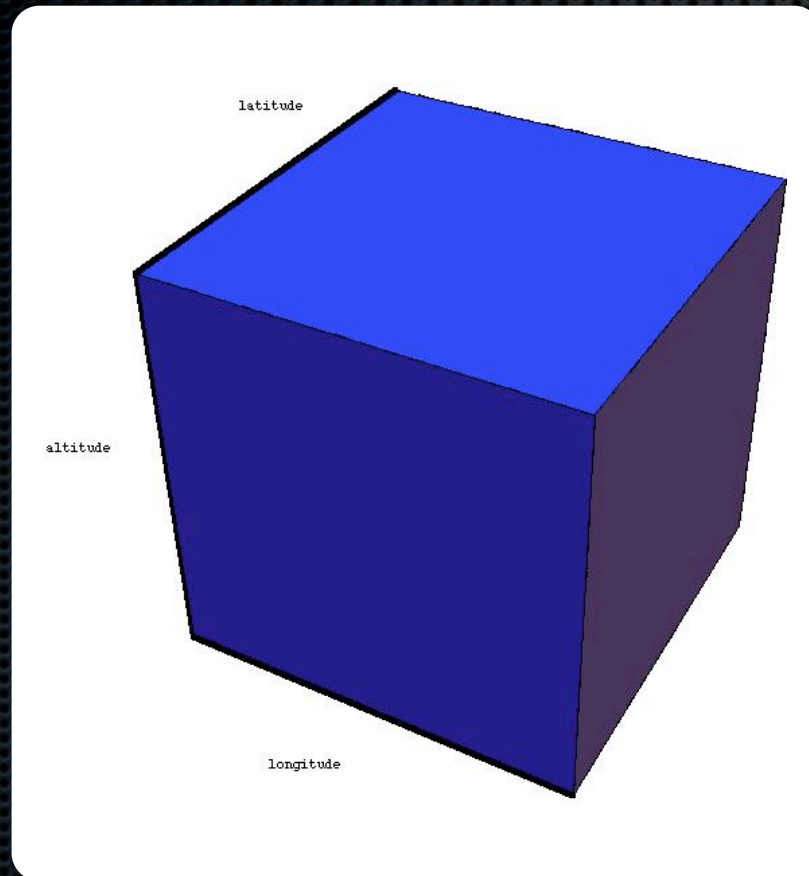


Note: vertical and horizontal axes are on different scales





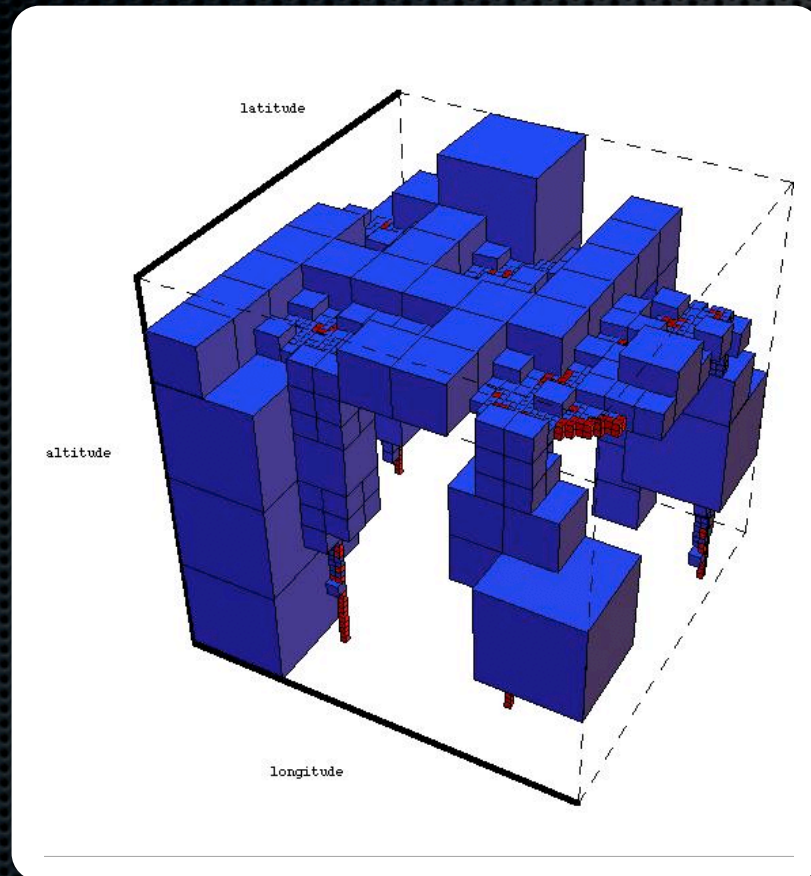
# Phase One: Priming the Octree



- The octree is populated by scheduling all expected missions
- Airspace is allocated without consideration of spatial constraints
- Red octants indicate resulting areas of contention



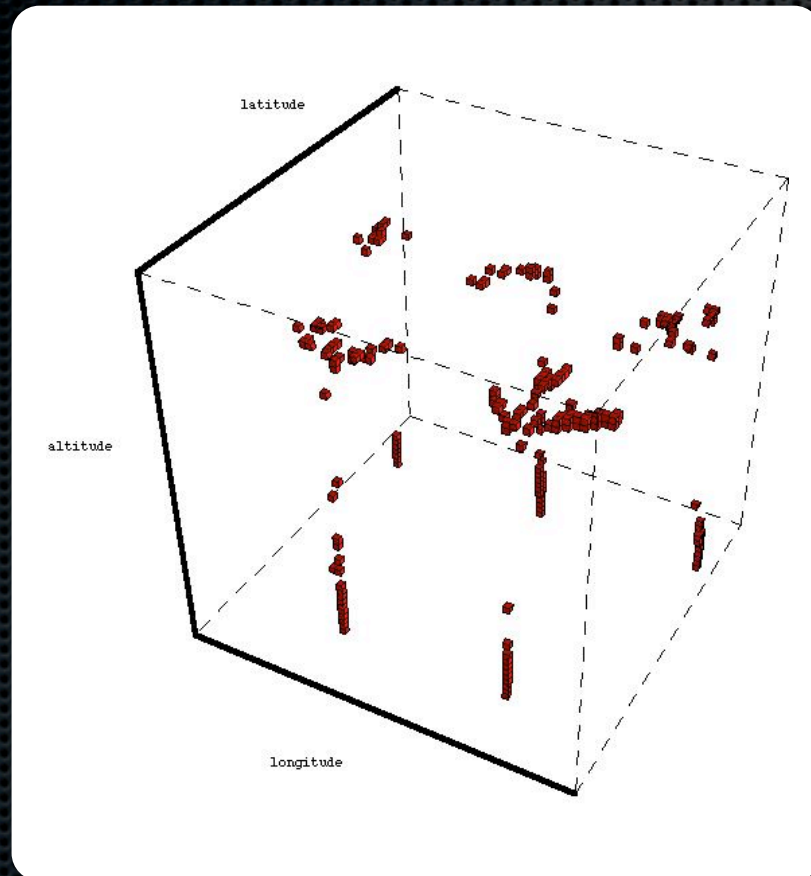
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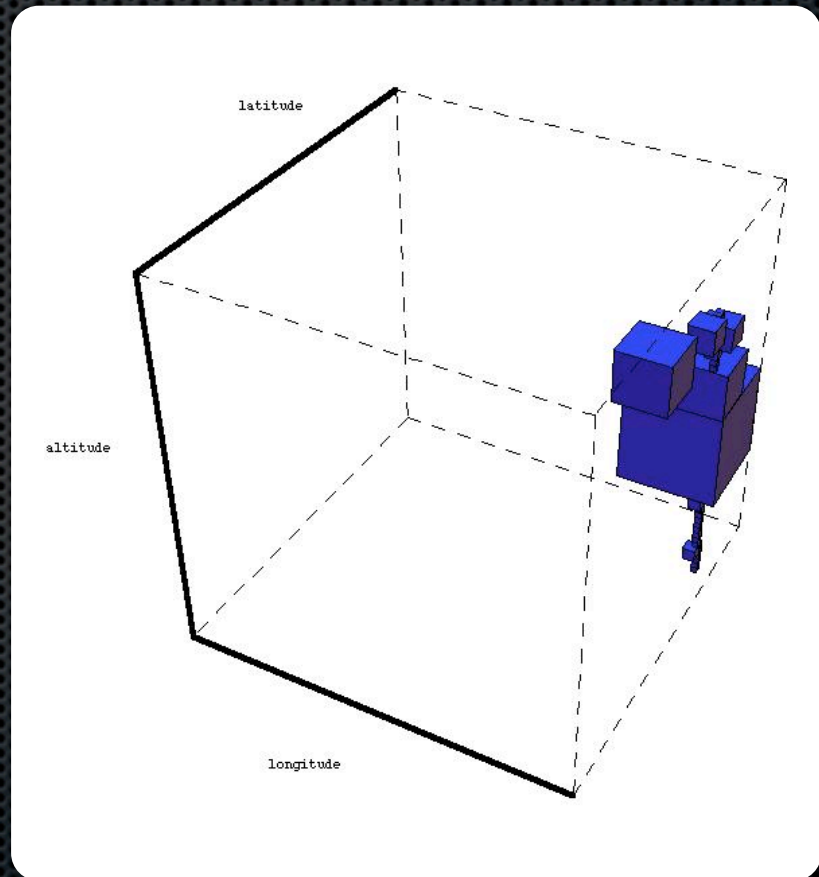


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# Phase Two: Deconfliction Scheduling

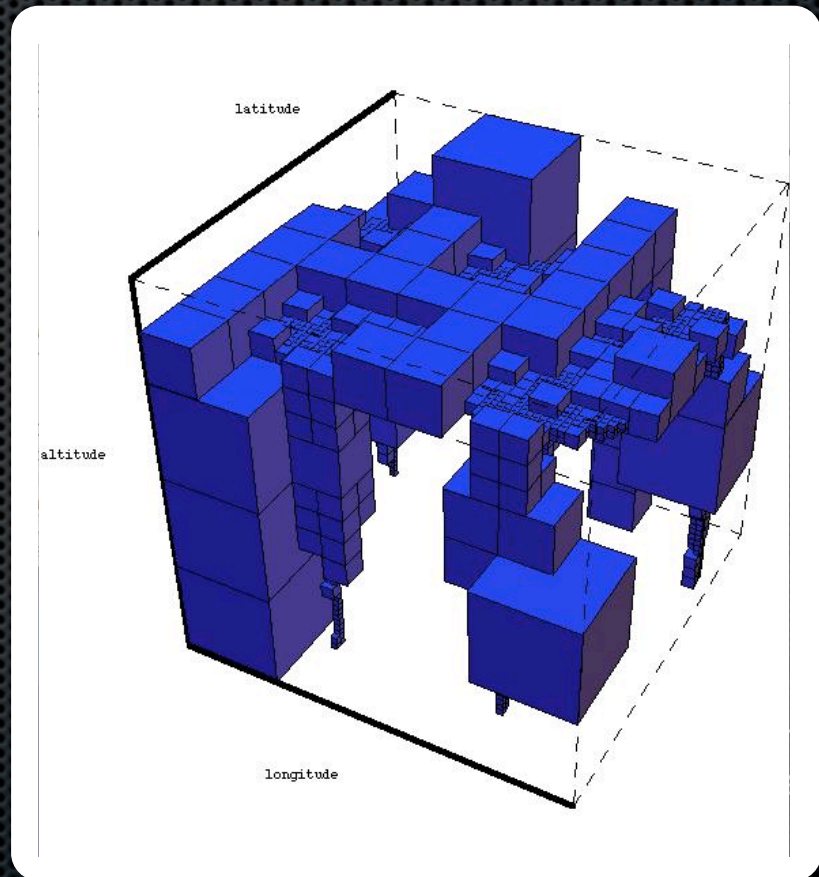
- The primed octree is used to guide the construction of a conflict-free schedule
- Traffic is directed to uncongested areas
- Routes are modified as necessary to avoid conflicts with other vehicles





# Phase Two: Deconfliction Scheduling

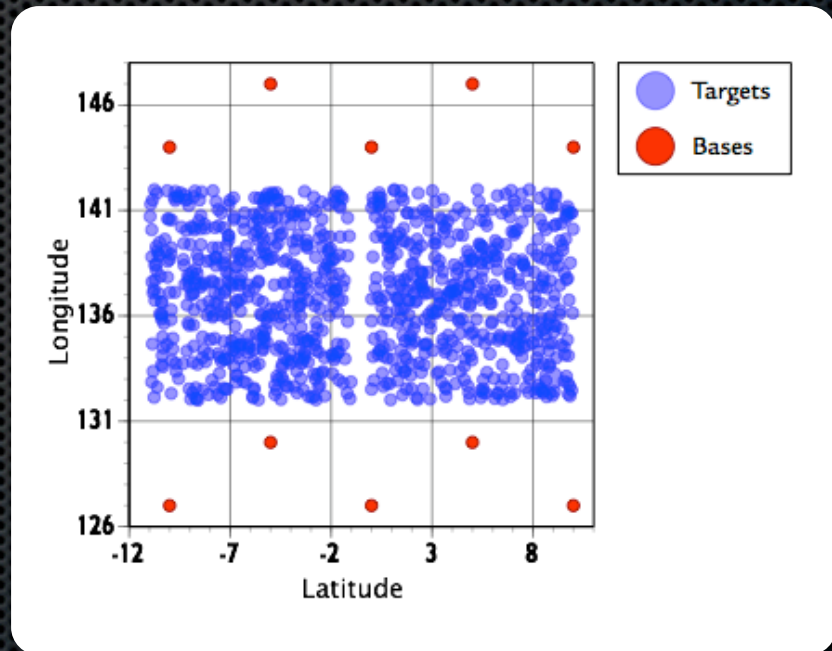
- The primed octree is used to guide the construction of a conflict-free schedule
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# Evaluation: The Problem Set

- 20 data sets
  - 50 to 1000 randomly generated targets (in increments of 50)
  - Two 700-miles-square target areas
  - 10 identically equipped bases





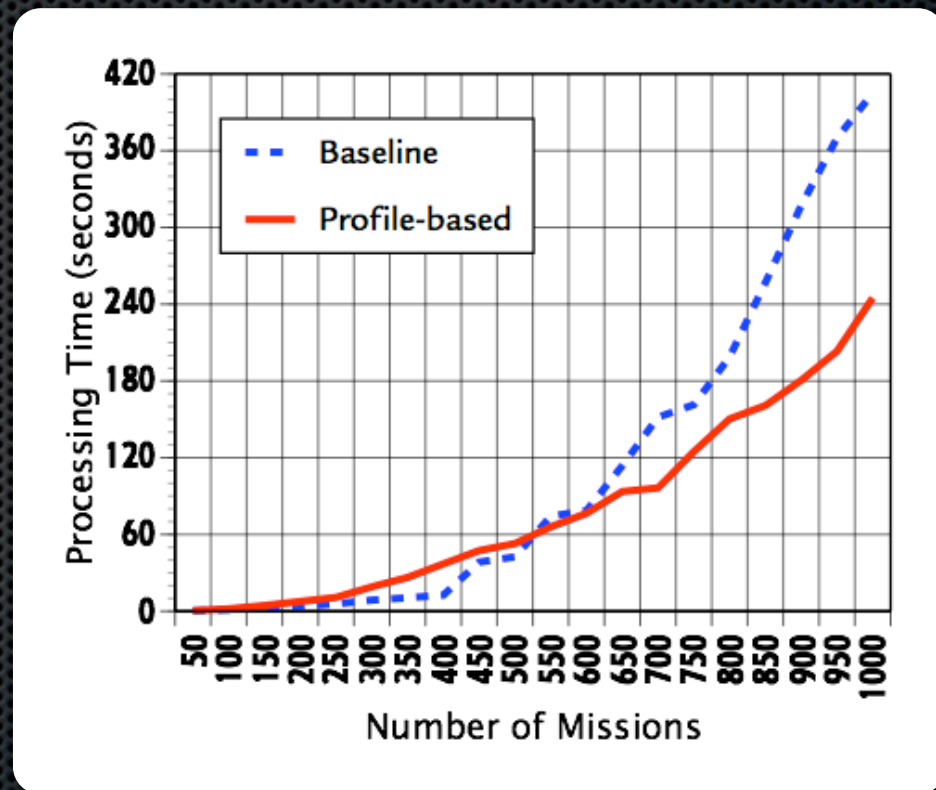
# Evaluation: Two Deconfliction Strategies

- **Baseline Approach**
  - No primed octree (**myopic**): if a conflict is detected, an attempt is made – based on the current partial state – to deconflict through route modification
- **Profile-based Approach**
  - Create and utilize the primed octree to guide route modification in response to conflicts



# Evaluation: Results

- Additional overhead for building the spatial contention profile is compensated for by an improvement in overall scheduling performance for sufficiently sized runs

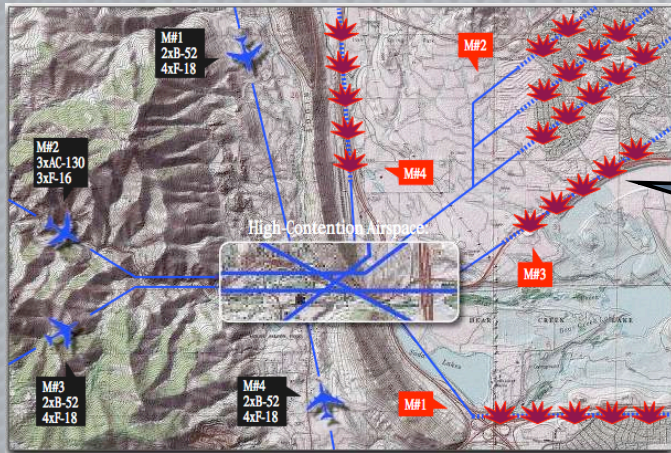




# Multi-Level Airspace Deconfliction Framework

## Airspace Sensitive, Multi-Mission Scheduling

- Mission trajectories, timings
- Potential conflicts



**Predictive Guidance  
(Potential Conflicts)**



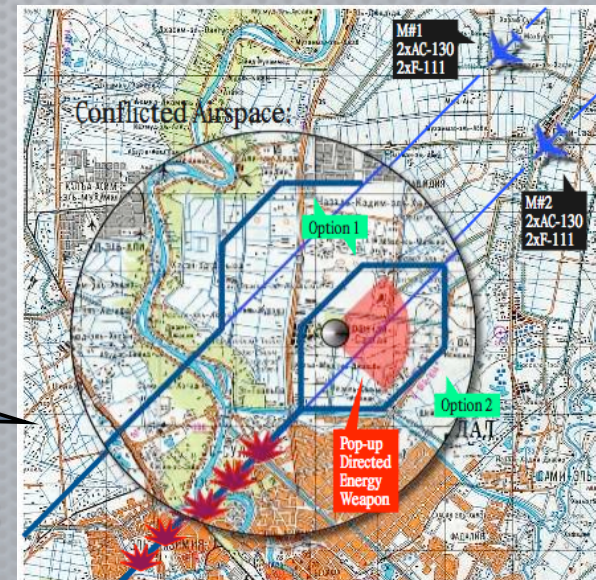
**Myopic Avoidance  
Actions**



**Downstream Impact**

## Distributed Real-time Airspace Deconfliction

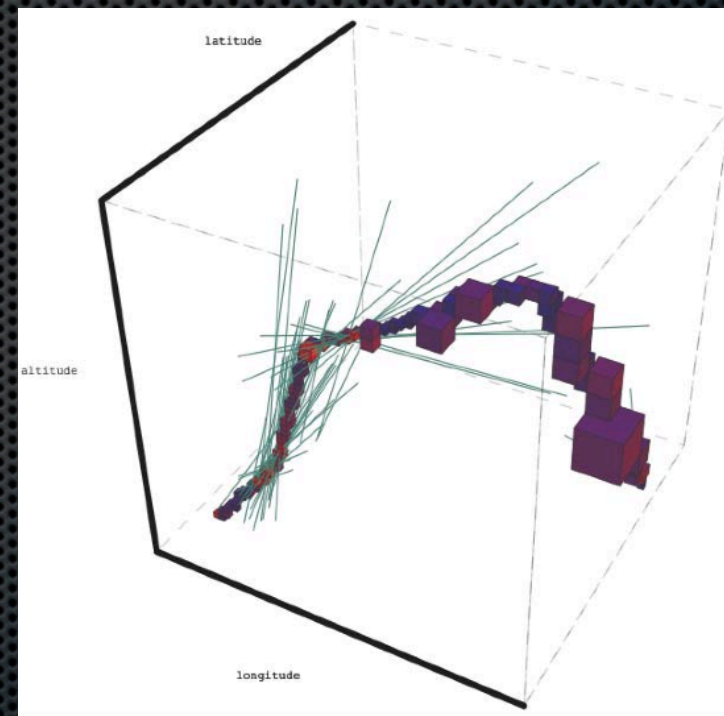
- Turn left, slow down





# Integrating with Real-Time Deconfliction Processes

- Use globally computed information to drive local deconfliction processes
  - Routes (i.e., sequences of waypoints)
  - Potential Conflicts (time and location)
  - Airspace Volume (given a 3D/4D region, where is the traffic?)
  - Airspace Corridor (are there sequences of under-populated 3D regions over time?)



*An example query: given a route, determine its traversed octants and all conflicting vectors (in green)*



# Operating Concept

- Distributed airborne processes assume responsibility for local deconfliction at execution time
- Global guidance is computed to provide an appropriate envelope of operations
- When any local route change is made, a query is made to the global scheduler to determine downstream impact and re-compute guidance

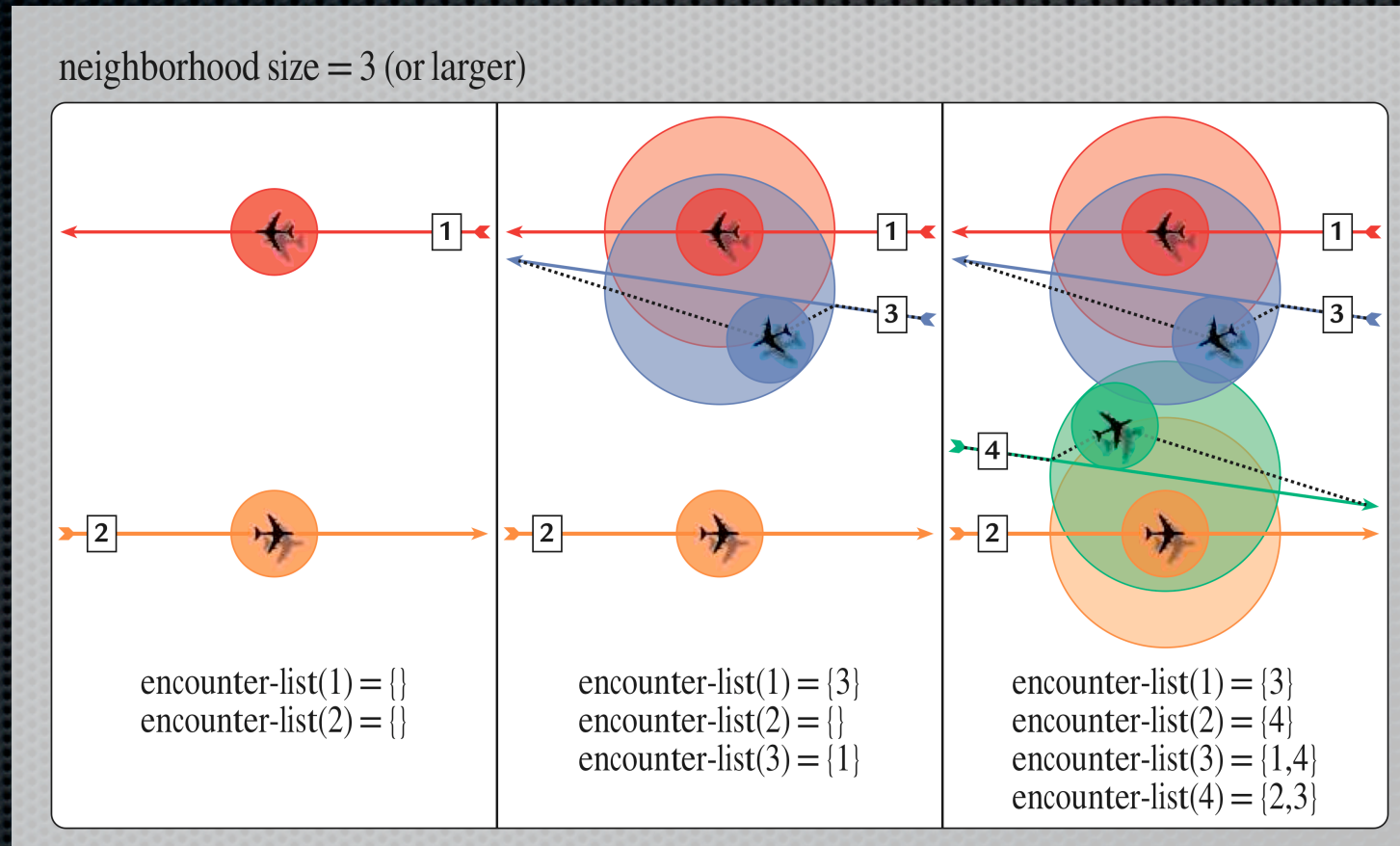


# Computing Potential Conflicts

- *Neighborhood size* – the number of aircraft allowed to simultaneously violate separation constraints within an octant before a conflict is signaled
- *Encounter region* – the sum of the separation constraint and the distance a vehicle is allowed to deviate from its path to avoid a conflict
- *Encounter list* – for a given neighborhood size  $>1$ , the set of other air vehicles falling within the encounter region of a given aircraft's itinerary. This list constitutes the set of potential conflicts.



# Encounter Lists





# Status

- Initial, distributed deconfliction process operational (running in simulation)
  - Formulated as a distributed constraint satisfaction problem
  - Protocol for conflict resolution via cooperative partial centralization
  - Encounter lists determine who to interact with
- XML API in place for requesting and communicating global guidance



# Future Directions

- Expansion of the spatial constraint model
- Consideration of more real-world constraints (e.g., maneuverability, fuel)
- Strategic analysis of conflict trajectories
- More sophisticated search and optimization procedures



# Reference

- D. W. Hildum and S. F. Smith, “Constructing Conflict-Free Schedules in Space and Time”, *Proceedings 17<sup>th</sup> International Conference on Automated Planning and Scheduling (ICAPS-07)*”, Providence RI, September, 2007.